



Practical Governmental Voting with Unconditional Integrity & Privacy

Nan Yang & Jeremy Clark, Concordia University



BALLOT	
CONTEST 1 VOTE FOR ONE	
C	CANDIDATE 1 PARTY 1
A	CANDIDATE 2 PARTY 2
B	CANDIDATE 3 PARTY 3
<p>(B) (C) (A)</p>	
SERIAL No:	1234-5678

Unconditional Integrity

A corrupt EA cannot undetectably manipulate ballots

- * Fully collude
- * Learn all the secrets/keys
- * Break all the cryptographic assumptions

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Of course, ballot secrecy breaks completely

Everlasting Privacy

Receipt-Free Universally-Verifiable Voting with Everlasting Privacy*

Tal Moran and Moni Naor**

Department of Computer Science and Applied Mathematics,
Weizmann Institute of Science, Rehovot, Israel

Abstract. We present the first universally verifiable voting scheme that can be based on a general assumption (existence of a non-interactive commitment scheme). Our scheme is also the first receipt-free scheme to give “everlasting privacy” for votes: even a computationally unbounded party does not gain any information about individual votes (other than what can be inferred from the final tally).

Our voting protocols are designed to be secure against a malicious authority.

Everlasting Privacy

Ballot secrecy cannot be broken

- * Break all the cryptographic assumptions
- * (However collusion does break it)

And of course, integrity breaks completely

Integrity needs to last the lifetime of the election, while ballot secrecy should last centuries

door
 Jurjen Norbert Eelco Bos
 geboren te Leiden.

Reference	Privacy	Security	Robustness	Remarks
Cha81	RSA	RSA	RSA	Privacy depends on batch size
DLM82	Pub. key	Pub. key	No	Difficult to comprehend
Yao82	Uncond.	Pub. key	No	
CF85	Residue	RSA	RSA	No privacy from government
Cha88	Uncond.	RSA	DC	DC system
Ben87	Residue	Residue	Uncond.	privacy \leftrightarrow robustness tradeoff
UT88	Uncond.	Priv. key	Priv. key	Needs secure private channels
Present	Uncond.	D. log.	DC	DC system

Table 3: Comparison of voting schemes.

Unconditional
Integrity

Unconditional
Ballot Secrecy

Unconditional Integrity

Punchscan
Scantegrity
Pret a Voter
Helios
JCJ/Civitas/Variants
STAR Voting

Unconditional Ballot Secrecy

Chaum 88
Kiayias-Yung
Moran-Naor
Demirel et al
Locher et al

You can have both

Information-Theoretically Secure Voting Without an Honest Majority

Anne Broadbent and Alain Tapp

Département d'informatique et de recherche opérationnelle
Université de Montréal, C.P. 6128, Succ. Centre-Ville
Montréal (QC), H3C 3J7 CANADA
{broadbea, tappa}@iro.umontreal.ca

Abstract. We present three voting protocols with unconditional privacy and information-theoretic correctness, without assuming any bound on the number of corrupt voters or voting authorities. All protocols have polynomial complexity and require private channels and a simultaneous broadcast channel. Our first protocol is a basic voting scheme which allows voters to interact in order to compute the tally. Privacy of the tally is unconditional, but any voter can cause the protocol to abort. Our second protocol introduces a commitment phase, and our third protocol introduces a decommitment phase.

You can have both

“We present three with unconditional privacy and information-theoretic correctness...”

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You can have both*

“We present three with unconditional privacy and information-theoretic correctness...”

Information-Theoretically Secure Voting Without an Honest Majority

Anne Broadbent and Alain Tapp

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*kind of

Info-Theoretic Secure

Unconditional Integrity & Everlasting Privacy

- * Voters participate in tallying the result
- * Essentially a big MPC with ballots as private inputs
- * “Boardroom Voting” - lots of earlier papers

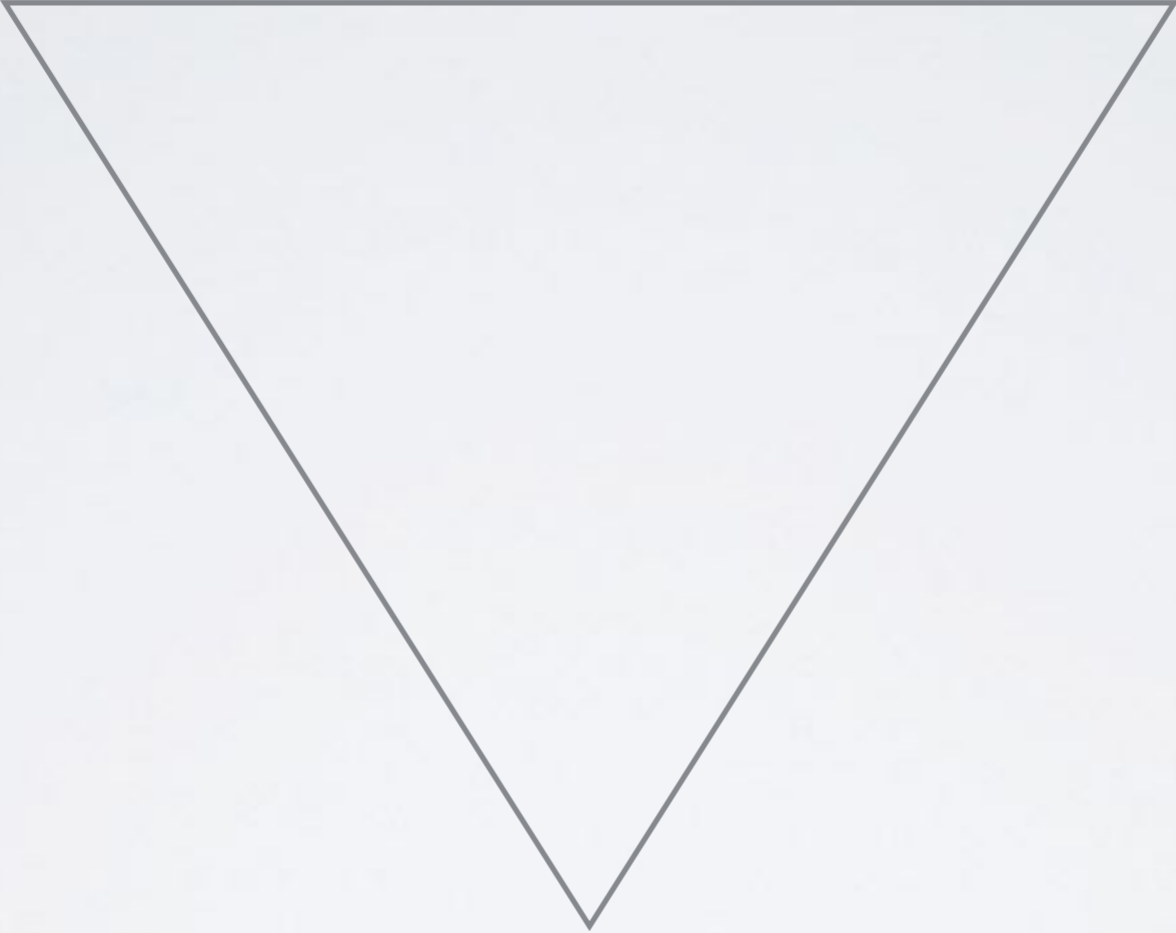
Governmental Elections

- * Human voteable
- * Vote-and-go

Can you have it all? Probably not, it is 2017 after-all

Unconditional
Integrity

Unconditional
Ballot Secrecy



?

An information-theoretic model of voting systems

Ben Hosp^{*}, Poorvi L. Vora

Department of Computer Science, George Washington University, Washington DC 20052, United States

Theorem. *A voting system cannot have perfect integrity, perfect privacy and perfect verifiability.*

Proof. Suppose the system has perfect integrity. That is, $V^\Sigma = \widehat{V}^\Sigma$. T —the truth of the statement $Tally = \widehat{v}^\Sigma$ —is hence the truth of the statement $Tally = v^\Sigma$. For perfect verifiability,

$$\begin{aligned} \mathcal{H}(T|P) &= 0 \quad \forall Tally \quad \forall p_{V^*} \\ \Rightarrow \mathcal{H}(V^\Sigma|P) &= 0 \quad \forall p_{V^*}. \end{aligned}$$

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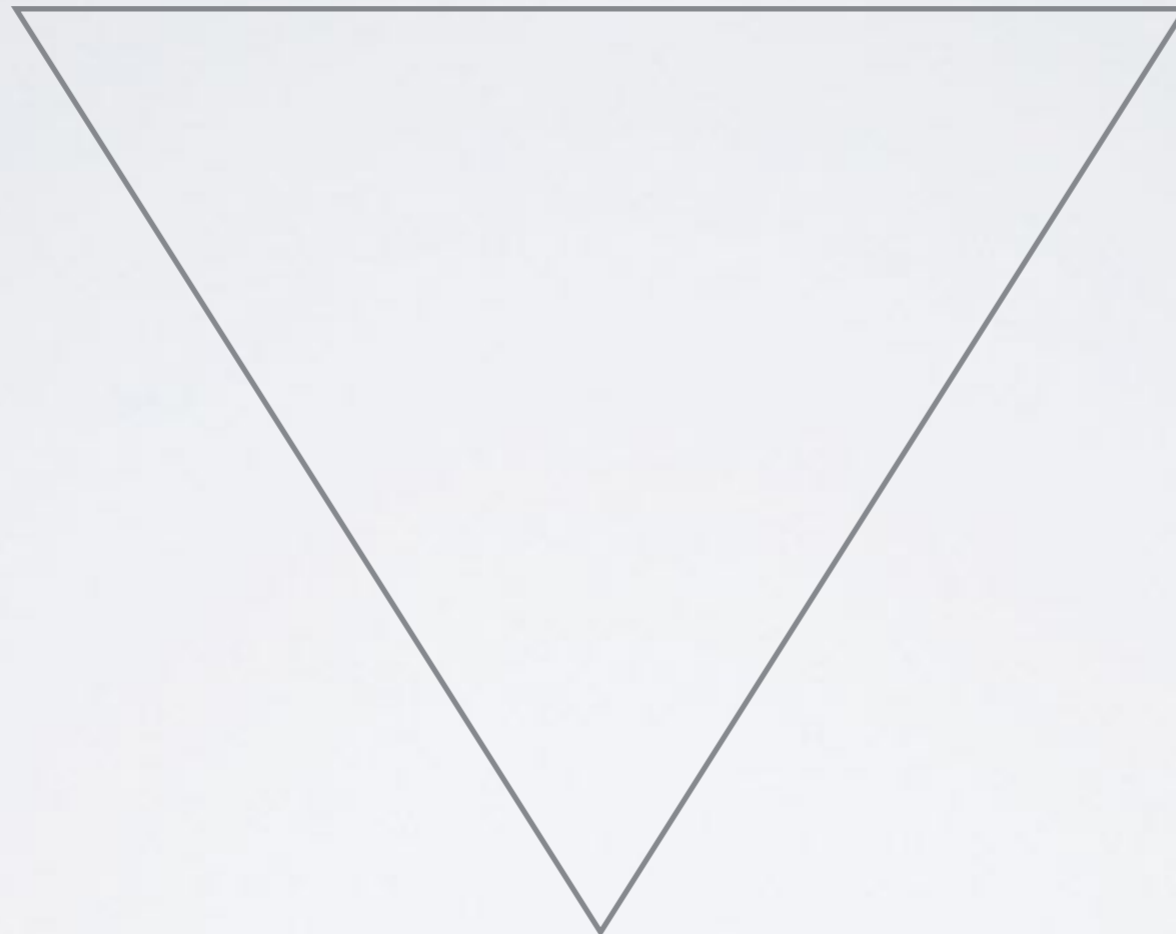
$$\begin{aligned} \mathcal{H}(T|P) &= 0 \quad \forall Tally \quad \forall p_{V^*} \\ \Rightarrow \mathcal{H}(V^\Sigma|P) &= 0 \quad \forall p_{V^*}. \end{aligned}$$

That is, all values of V^* and Y^* that satisfy the verified claims give the same value of V^Σ

Hosp-Vora Triangle

Unconditional
Integrity

Unconditional
Ballot Secrecy



Universal Verification

Hosp-Vora Triangle

Unconditional
Integrity

Unconditional
Ballot Secrecy

Most E2E Systems

Universal Verification

Hosp-Vora Triangle

Unconditional
Integrity

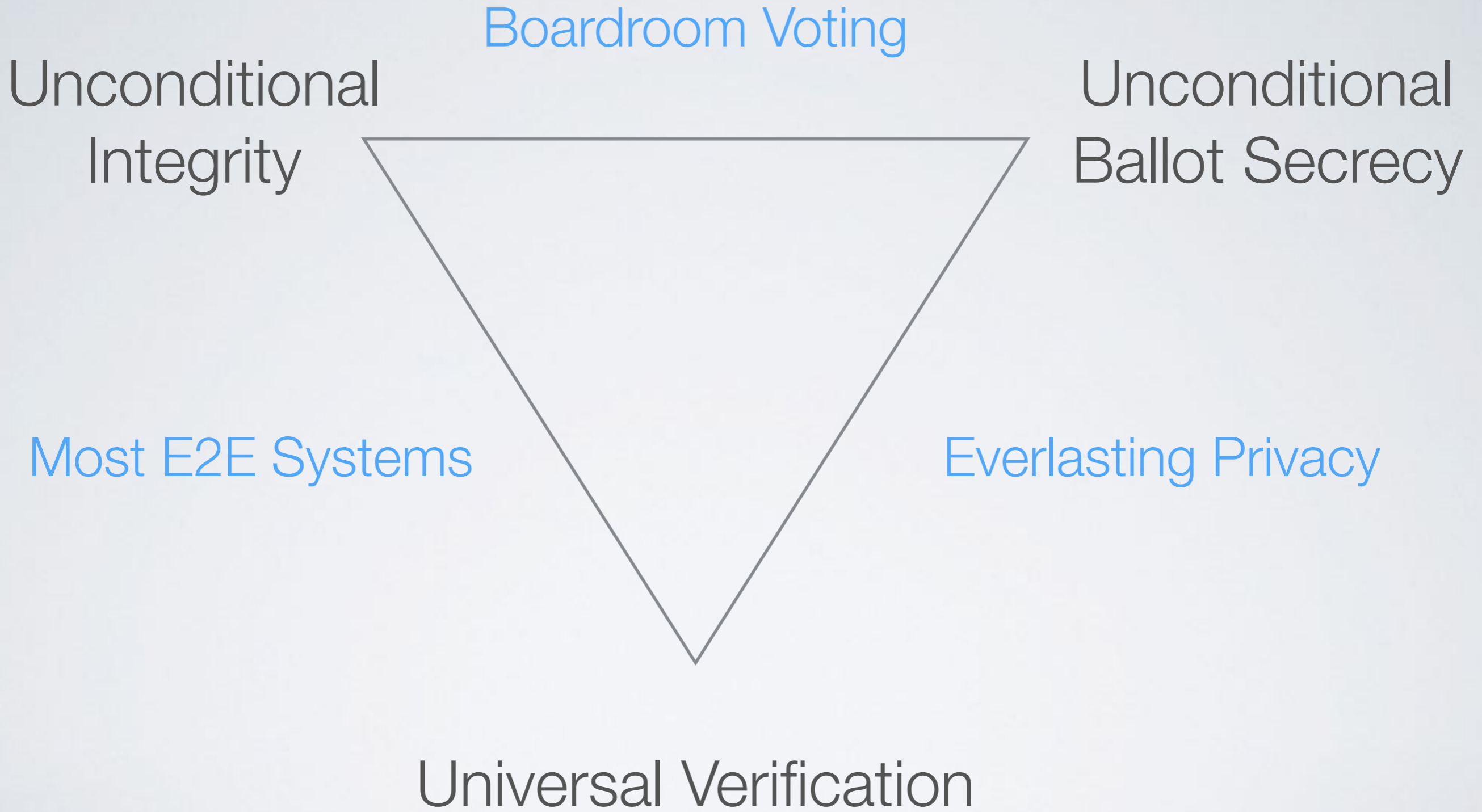
Unconditional
Ballot Secrecy

Most E2E Systems

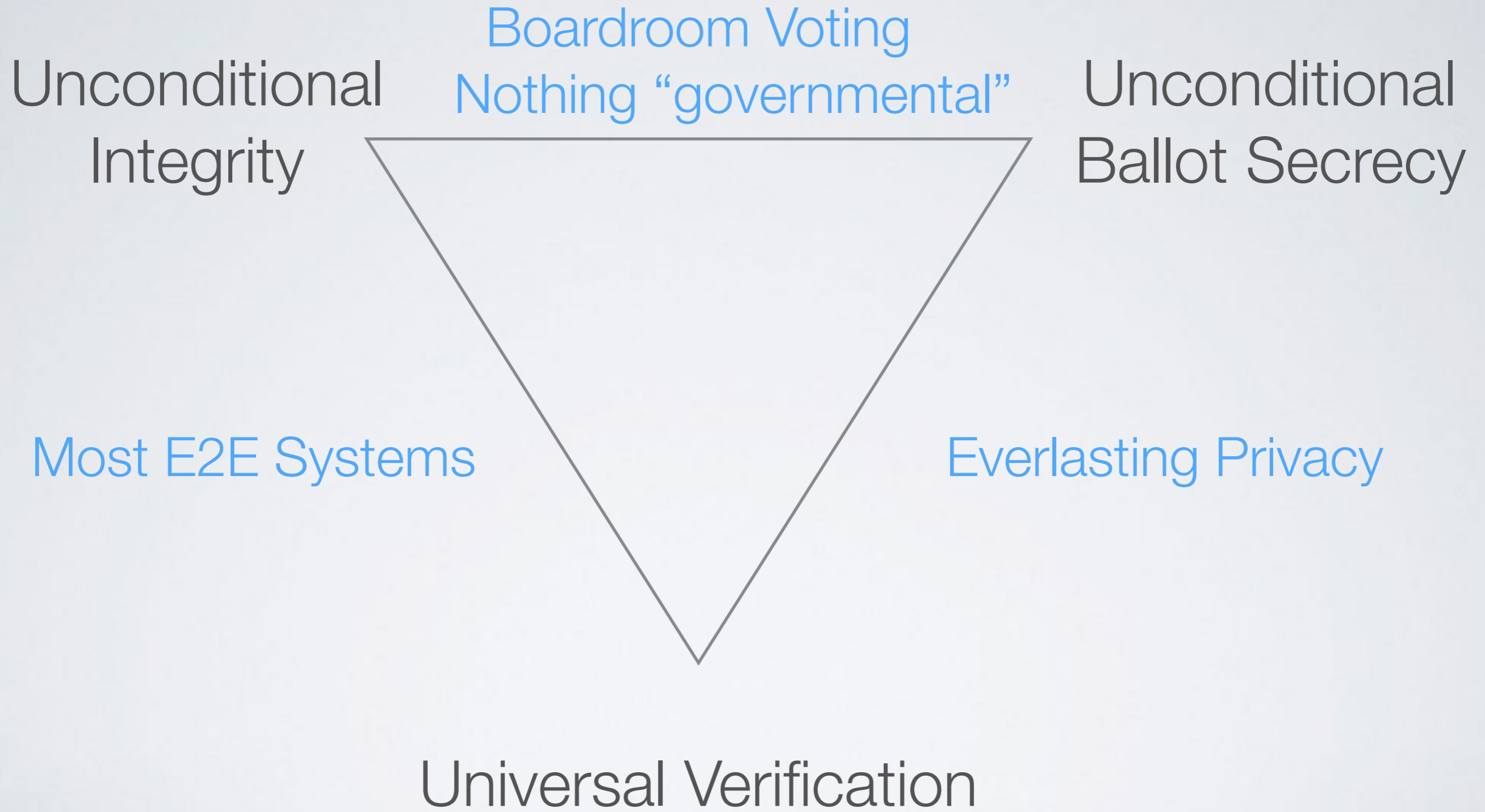
Everlasting Privacy

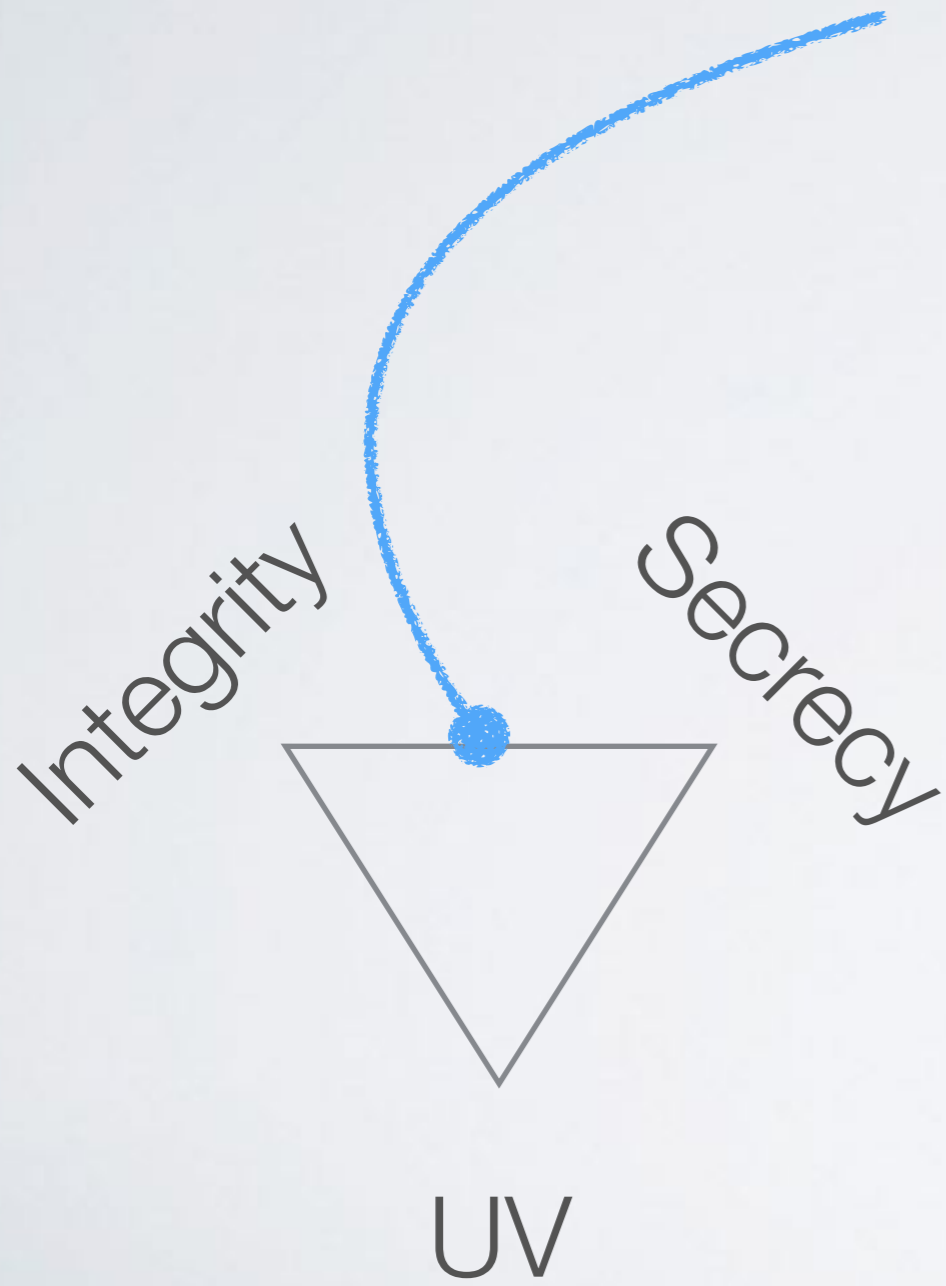
Universal Verification

Hosp-Vora Triangle

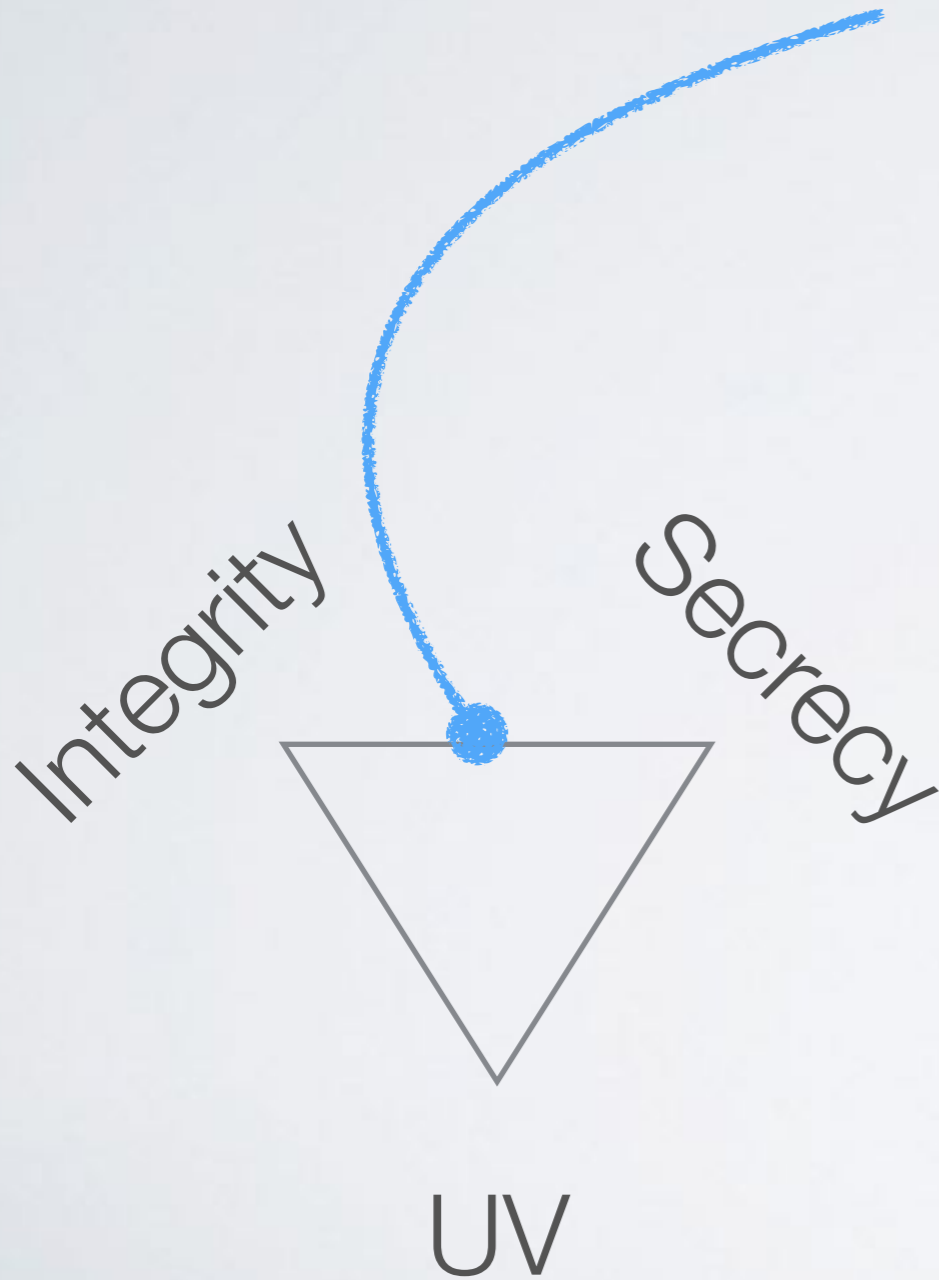


Hosp-Vora Triangle





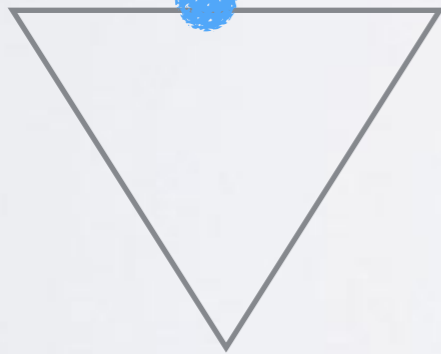
- + Human voteable
- + Vote-and-go



- + Human voteable
- + Vote-and-go

Integrity

Secrecy



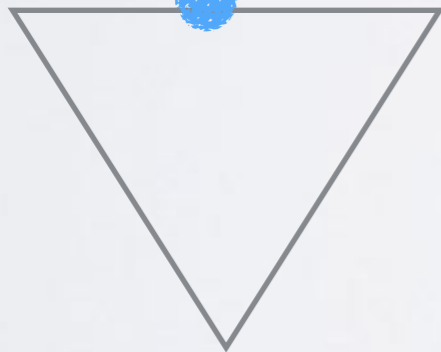
UV

E22 paper ballots

- + Human voteable
- + Vote-and-go

Integrity

Secrecy



UV

E22 paper ballots

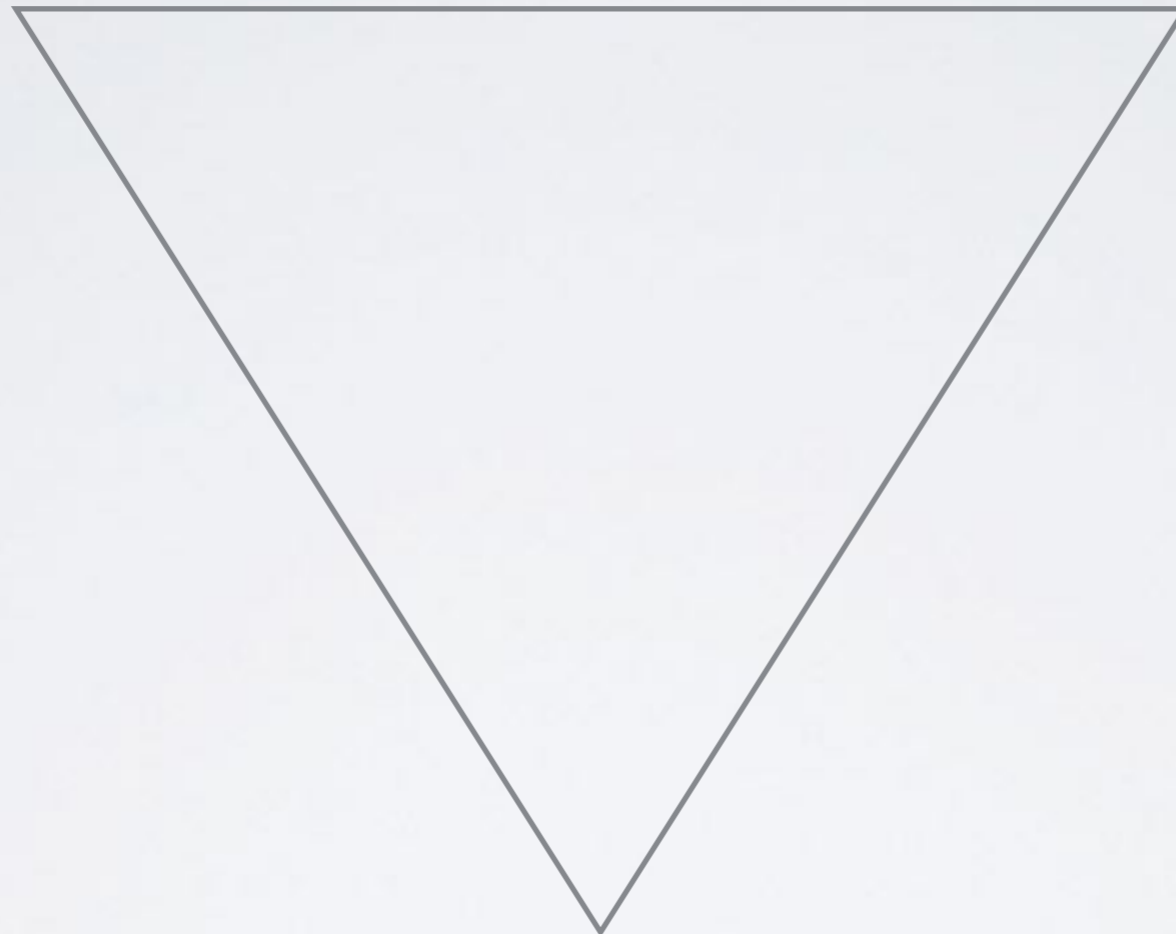
Obfuscation of the vote:

- * Commit / Encrypt
- * ZKPs

Vote Obfuscation

Unconditional
Integrity

Unconditional
Secrecy



Universal Verification

Vote Obfuscation

Unconditional
Integrity

Unconditional
Secrecy

Perfectly binding:

- * Elgamal
- * Paillier
- * Hash commit

Perfectly hiding:

- * Pedersen commit

Universal Verification

Vote Obfuscation

Secret Sharing

Unconditional
Integrity

Unconditional
Secrecy

Perfectly binding:

- * Elgamal
- * Paillier
- * Hash commit

Perfectly hiding:

- * Pedersen commit

Universal Verification

“VSS is... the distributed analogue of a commitment function”

Broadcast (and Round) Efficient Verifiable Secret Sharing*

JUAN GARAY**, CLINT GIVENS***, RAFAIL OSTROVSKY†, and PAVEL RAYKOV‡

Abstract. Verifiable secret sharing (VSS) is a fundamental cryptographic primitive, lying at the core of secure multi-party computation (MPC) and, as the distributed analogue of a commitment functionality, used in numerous applications. In this paper we focus on unconditionally secure VSS protocols with honest majority. In this setting it is typically assumed that parties are connected pairwise by authenticated, private channels, and that in addition they have access to a “broadcast” channel. Because broadcast *cannot* be simulated on a point-to-point network when a third or more of the parties are corrupt, it is impossible to construct VSS (and more generally, MPC) protocols in this setting without using a broadcast channel (or some equivalent addition to the model). A great deal of research has focused on increasing the efficiency of VSS, primarily in terms of round complexity. In this work we consider a refinement of the round complexity of VSS, by adding a measure we term *broadcast complexity*. We view the broadcast channel as an expensive resource and seek to minimize the number of rounds used in the protocol, as well. We construct a (linear-time) VSS protocol that uses only $O(n)$ broadcast complexity.

“VSS is... the distributed analogue of a commitment function”

Computationally it unconditionally secure (hiding and binding) however it requires an honest threshold of shareholders

Broadcast (and Round) Efficient Verifiable Secret Sharing*

JUAN GARAY**

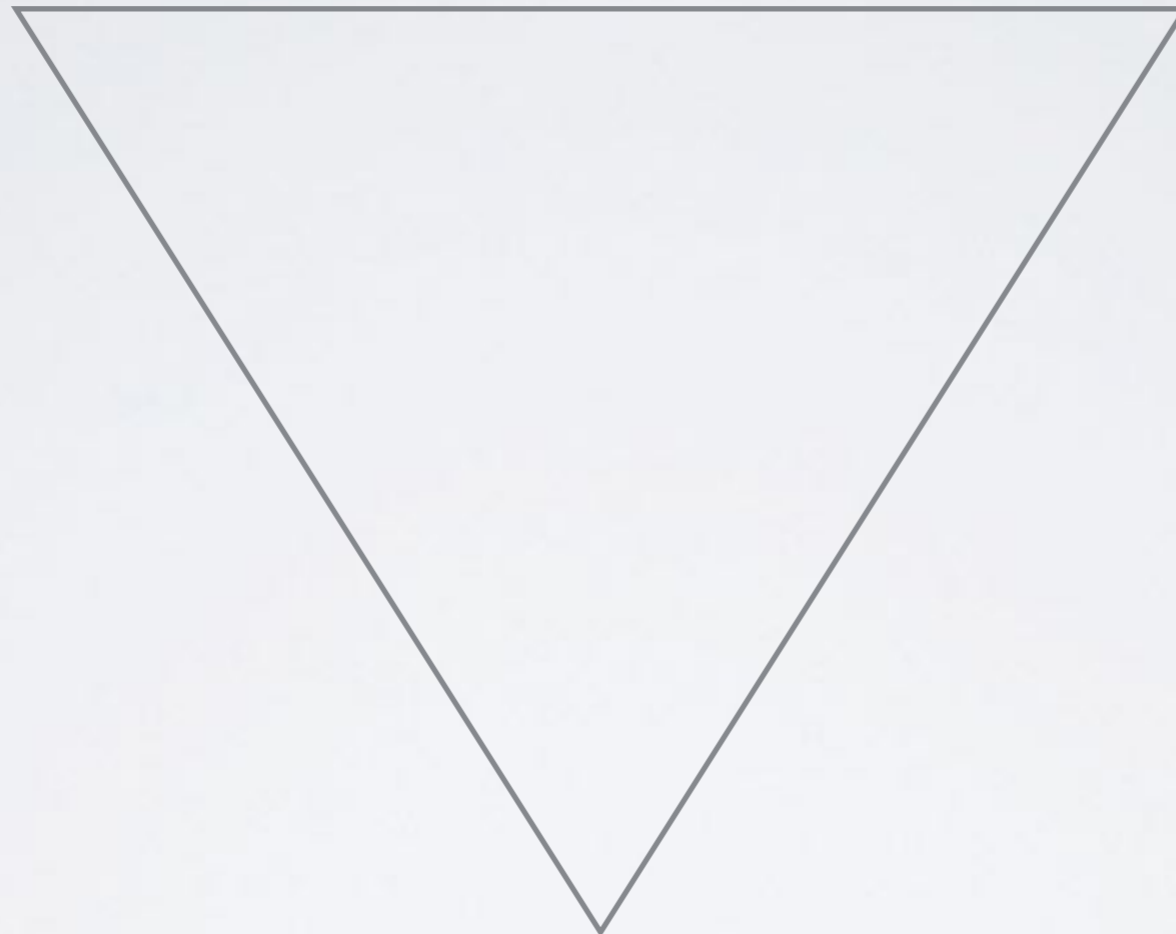
CLINT GIVENS***, DANIEL D. OLSH***, AND PAVEL

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Zero Knowledge

Unconditional
Integrity

Unconditional
Secrecy



Universal Verification

Zero Knowledge

?

Unconditional
Integrity

Unconditional
Secrecy

NIZKPs

ZK Arguments
ZK-SNARKS

Universal Verification

Zero Knowledge

ZKPs

Unconditional
Integrity

Unconditional
Secrecy

NIZKPs

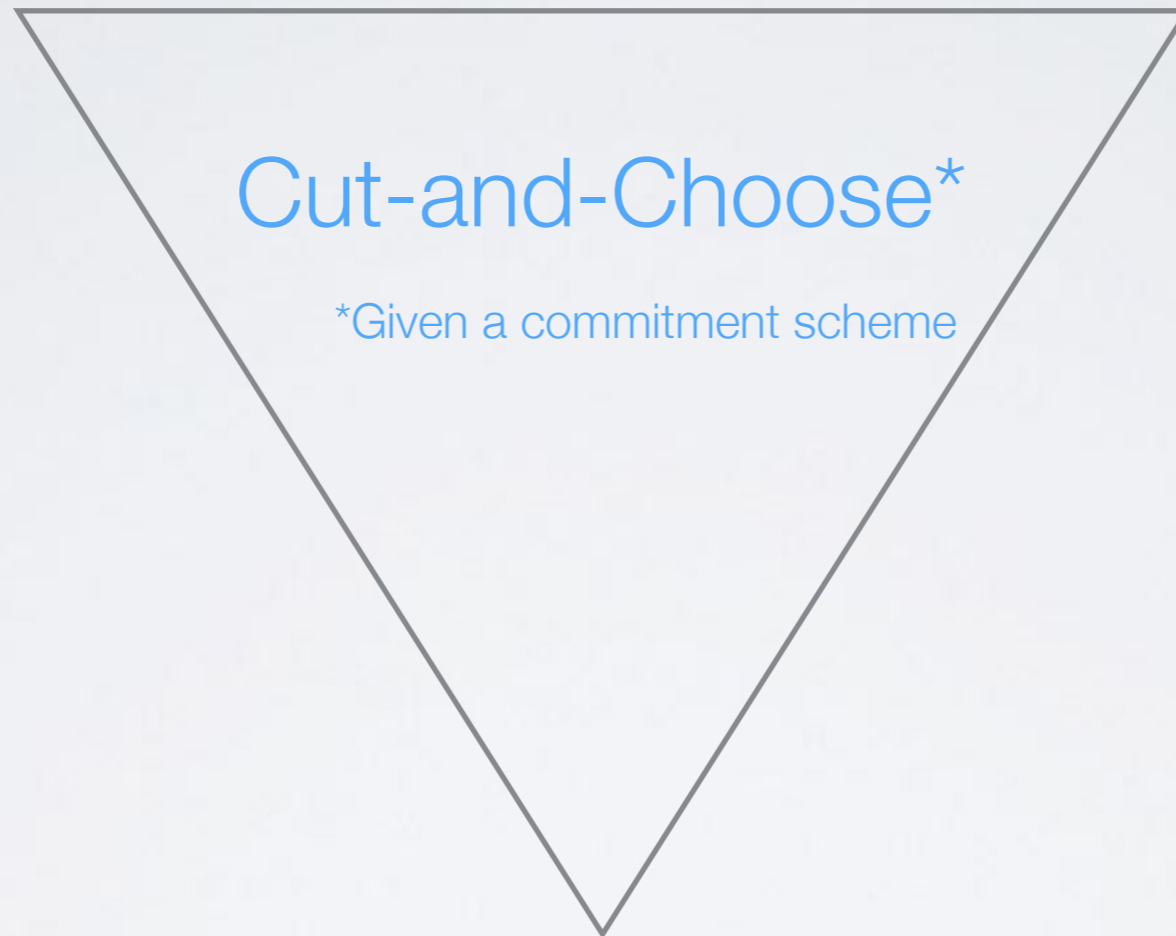
ZK Arguments
ZK-SNARKS

Universal Verification

Zero Knowledge

Unconditional
Integrity

Unconditional
Secrecy



Universal Verification

Wanted

Existing voting system:

- * Only relies on commitments
- * Uses cut-and-choose
- * Human-votable paper (or untrusted DRE) ballots
- * Voter not involved in tallying process

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- * Only relies on commitments
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Possible!

- * Punchscan
- * Scantegrity
- * Eperio (fast, easy, can do in a spreadsheet)

Wanted

Existing voting system:

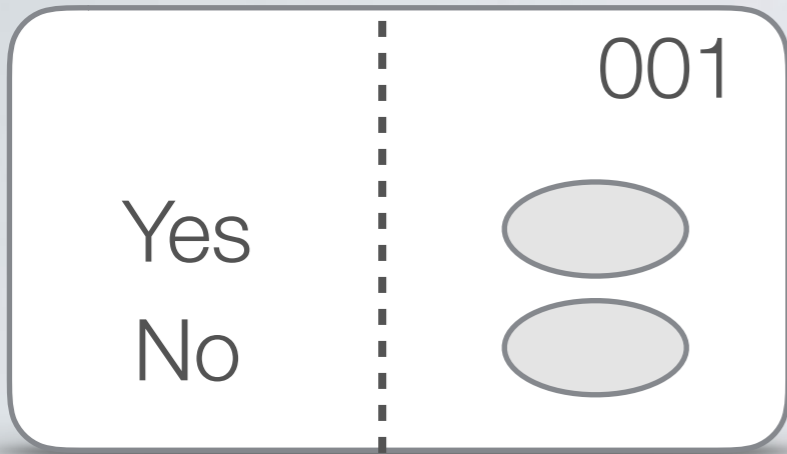
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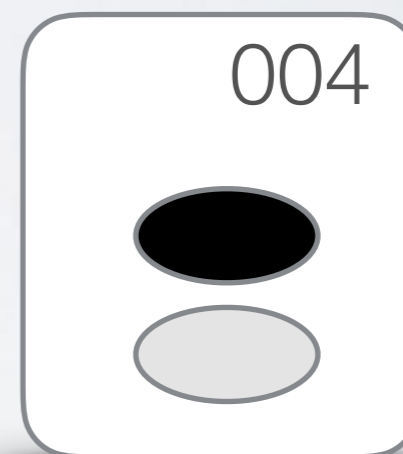
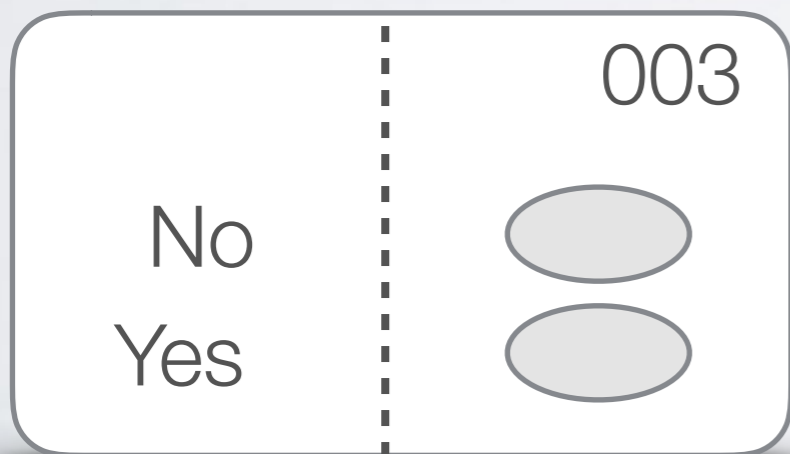
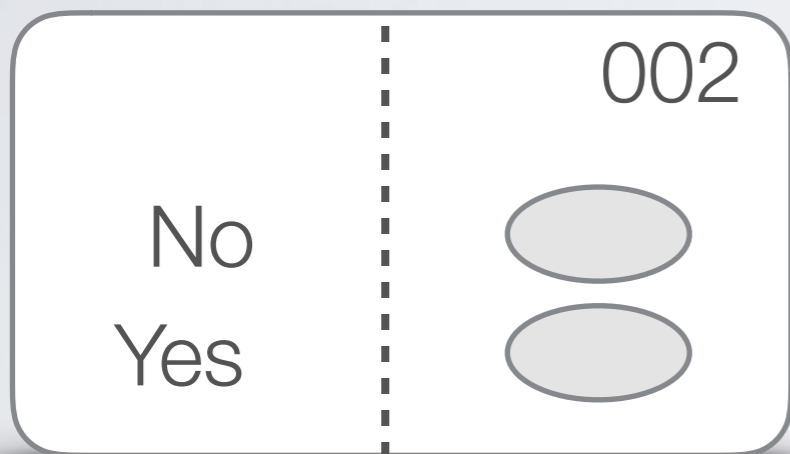
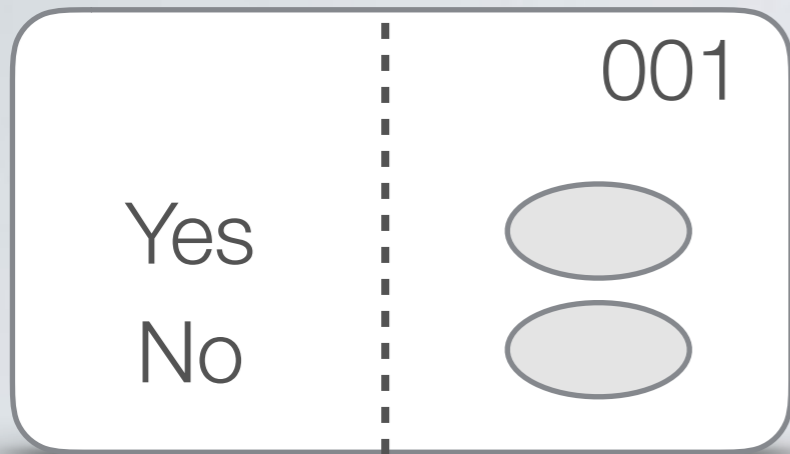
Possible!

- * Punchscan
- * Scantegrity
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The fine print

- * Black box assumption





001

Yes
No

002

No
Yes

003

No
Yes

001.1		Yes
001.2		No
002.1		No
002.2		Yes
003.1		No
003.2		Yes

001

Yes

No

002

No

Yes

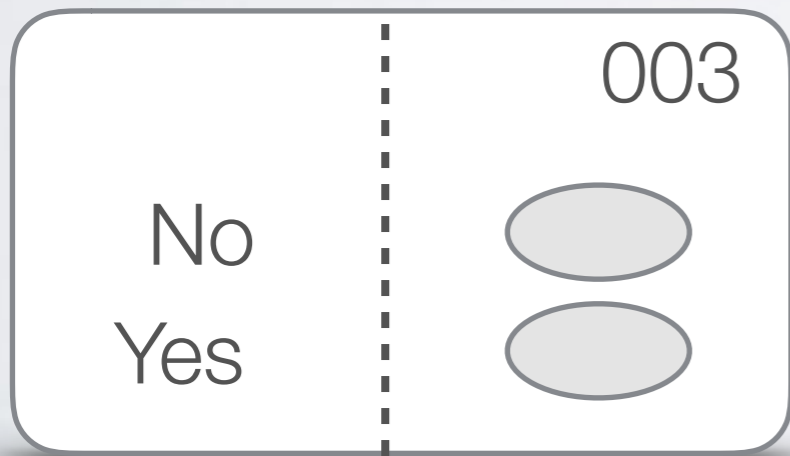
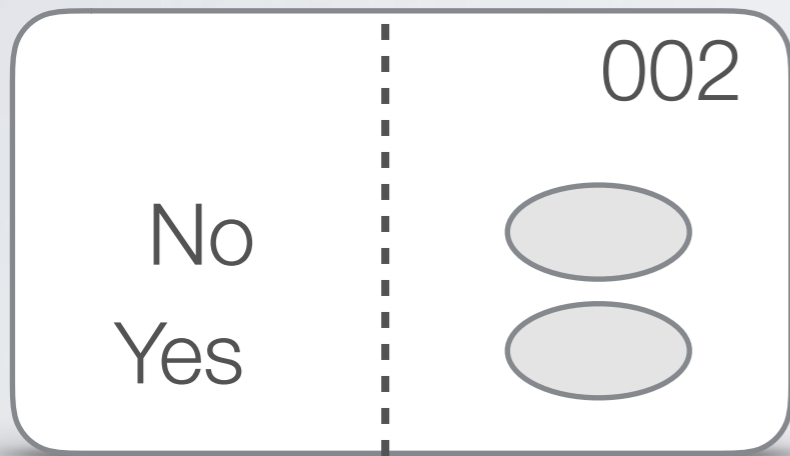
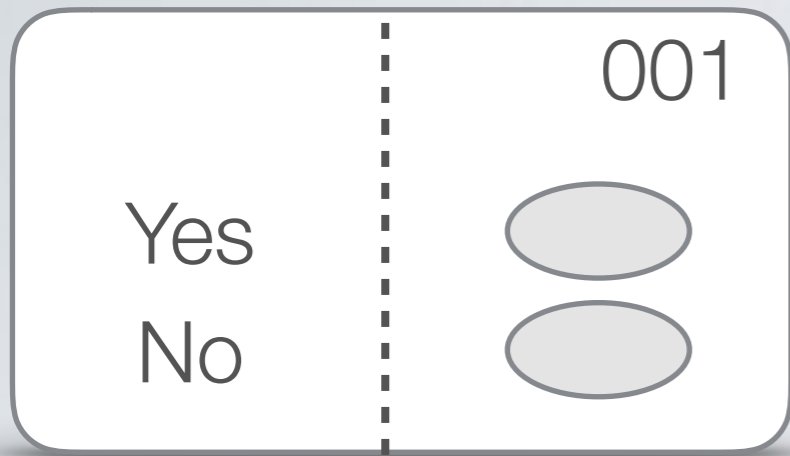
003

No

Yes

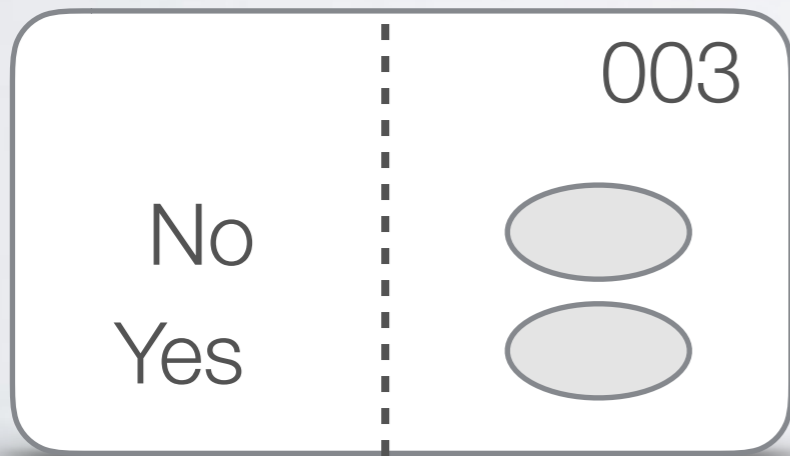
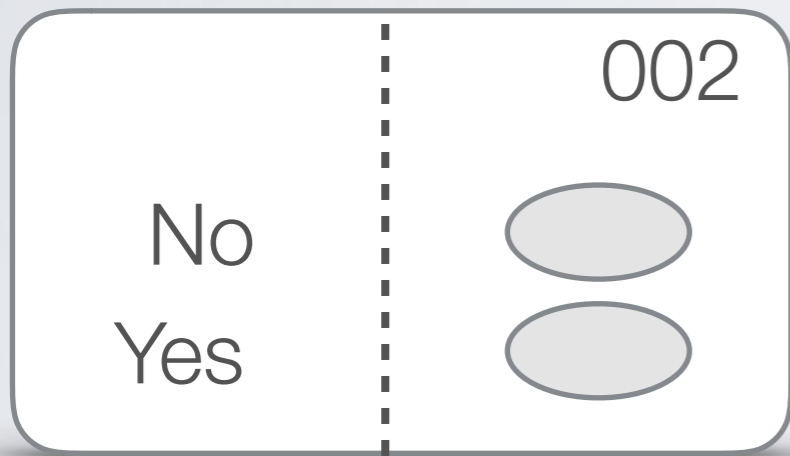
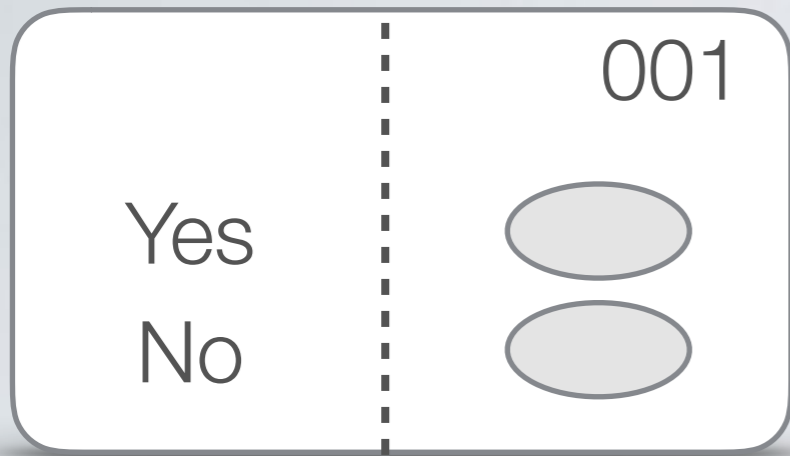
003.1		No
001.2		No
002.2		Yes
003.2		Yes
001.1		Yes
002.1		No

Blackbox



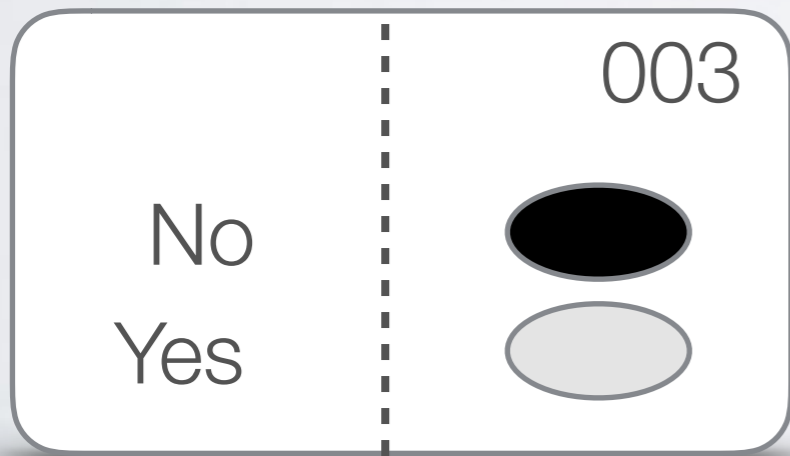
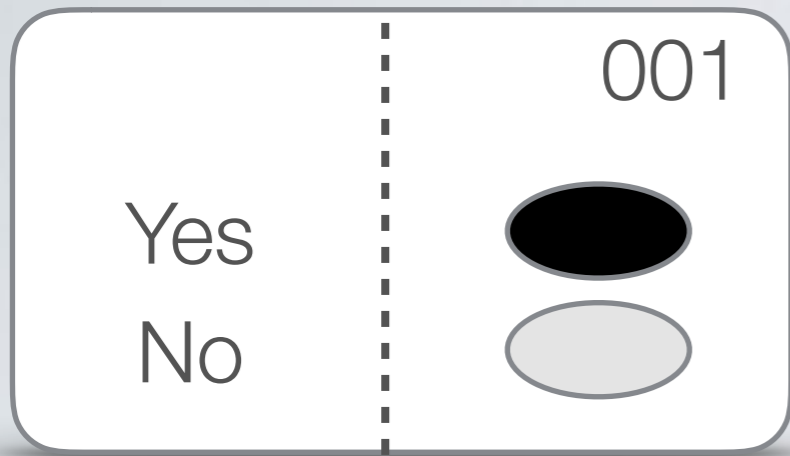
003.1		No
001.2		No
002.2		Yes
003.2		Yes
001.1		Yes
002.1		No

002.2		Yes
002.1		No
001.2		No
003.2		Yes
001.1		Yes
003.1		No



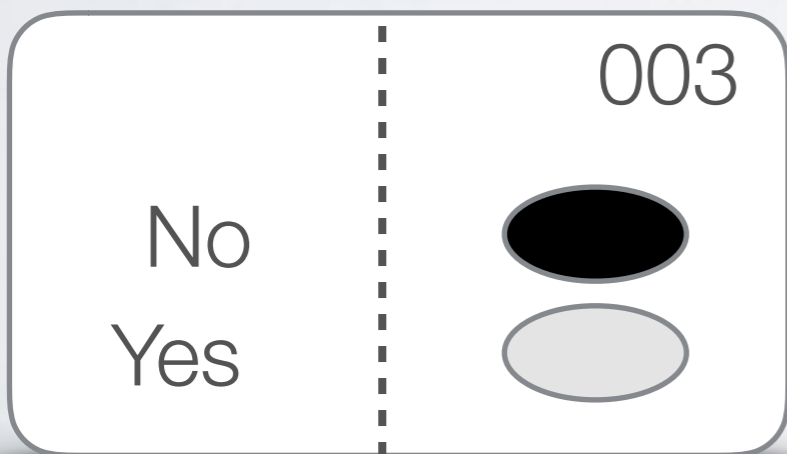
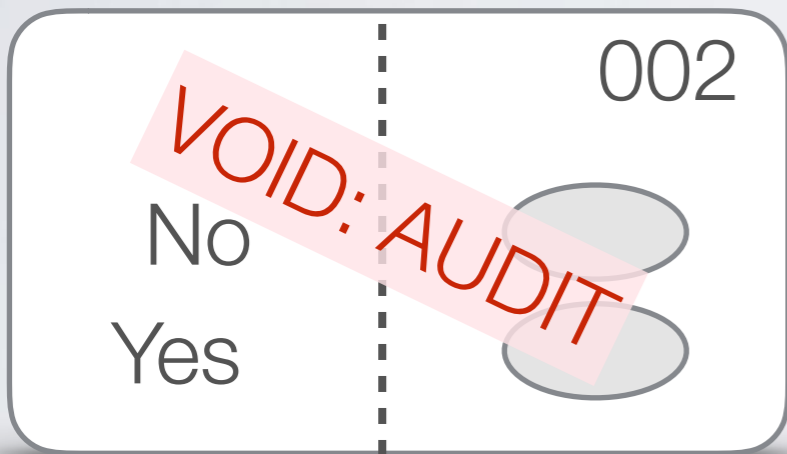
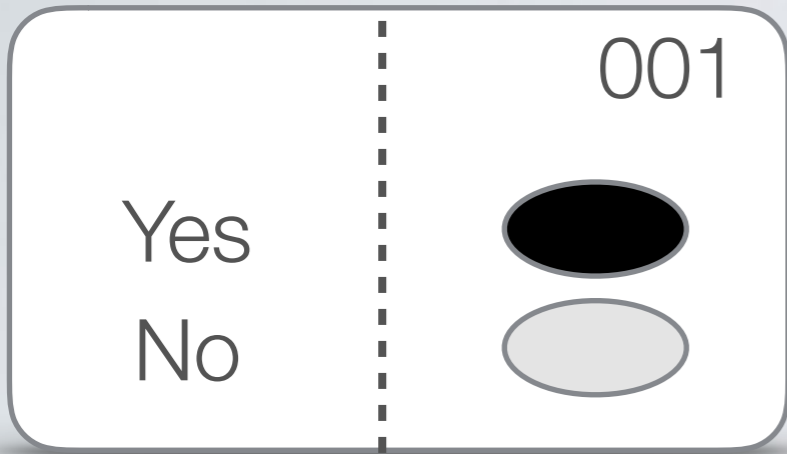
003.1		No
001.2		No
002.2		Yes
003.2		Yes
001.1		Yes
002.1		No

002.2		Yes
002.1		No
001.2		No
003.2		Yes
001.1		Yes
003.1		No



003.1		No
001.2		No
002.2		Yes
003.2		Yes
001.1		Yes
002.1		No

002.2		Yes
002.1		No
001.2		No
003.2		Yes
001.1		Yes
003.1		No



003.1	✓	No
001.2		No
002.2		Yes
003.2		Yes
001.1	✓	Yes
002.1		No

002.2		Yes
002.1		No
001.2		No
003.2		Yes
001.1	✓	Yes
003.1	✓	No

001

Yes

No

VOID: AUD

No

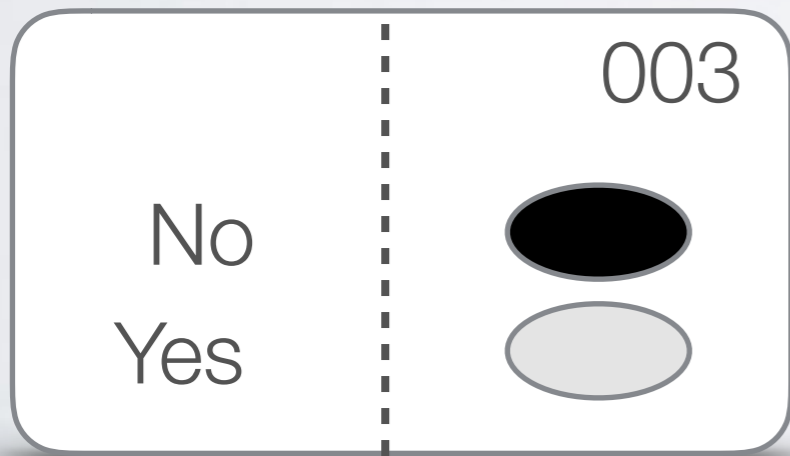
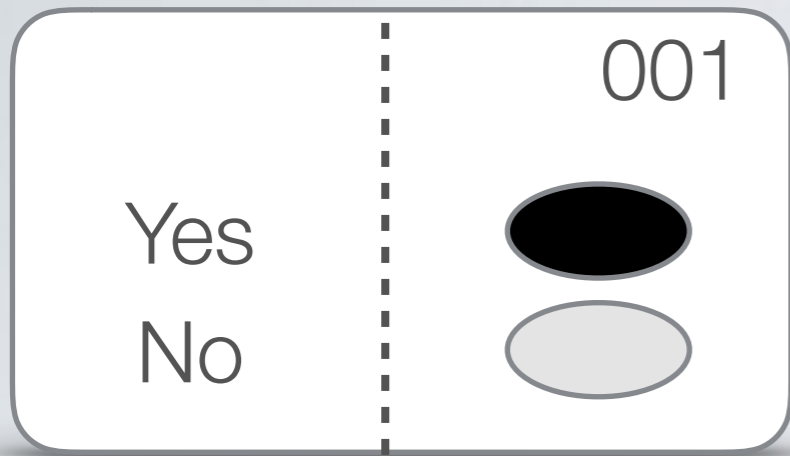
Yes

No

Yes

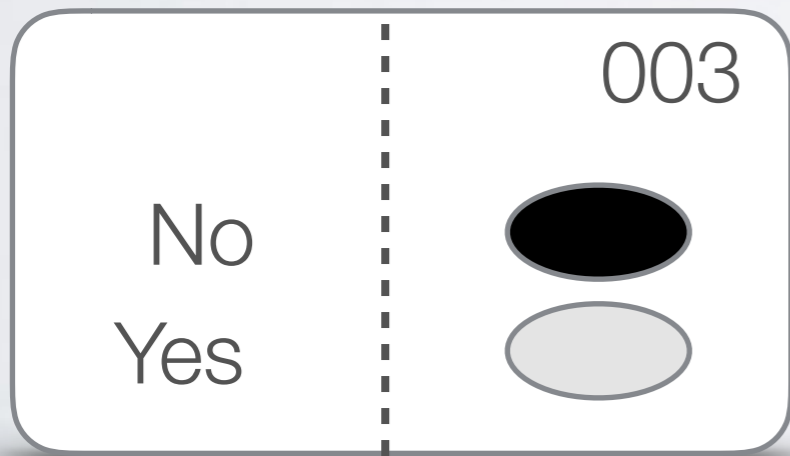
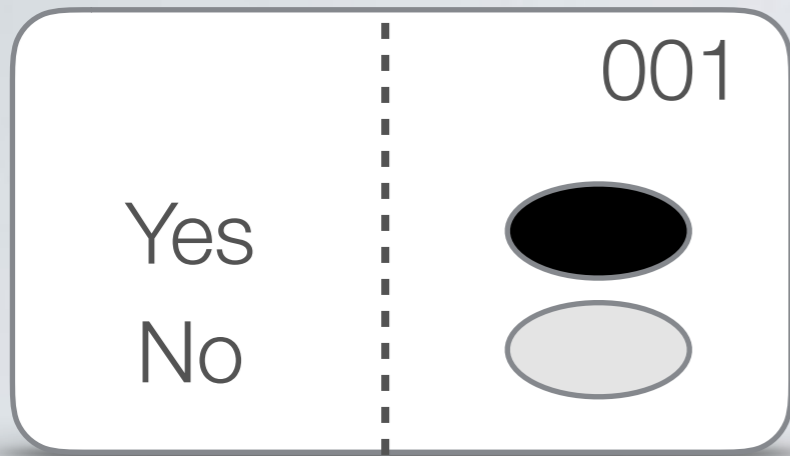


003.1	✓	No
001.2		No
002.2		Yes
003.2		Yes
	✓	Yes
		No
		Yes
		No
		No
003.2		Yes
001.1	✓	Yes
003.1	✓	No



003.1	✓	No
001.2		No
002.2		Yes
003.2		Yes
001.1	✓	Yes
002.1		No

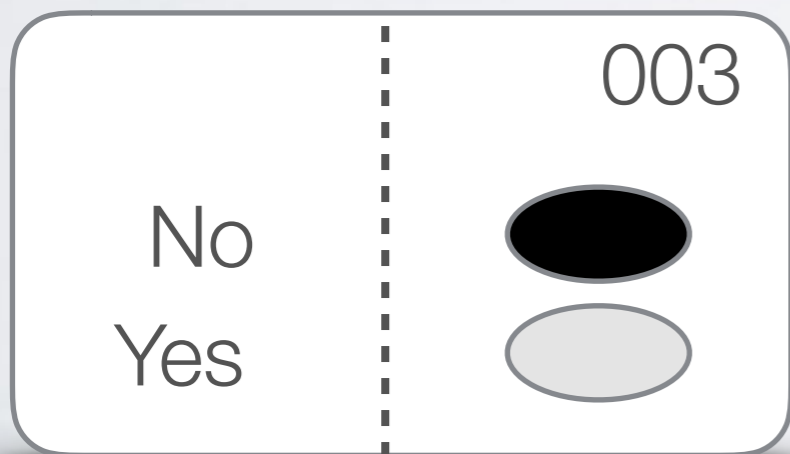
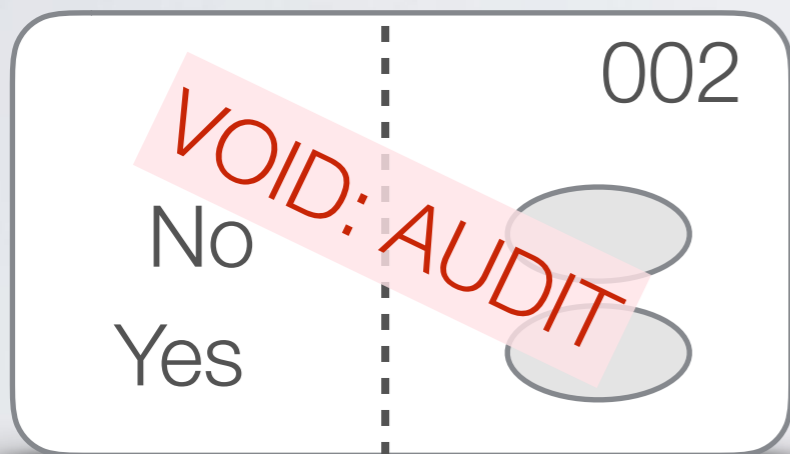
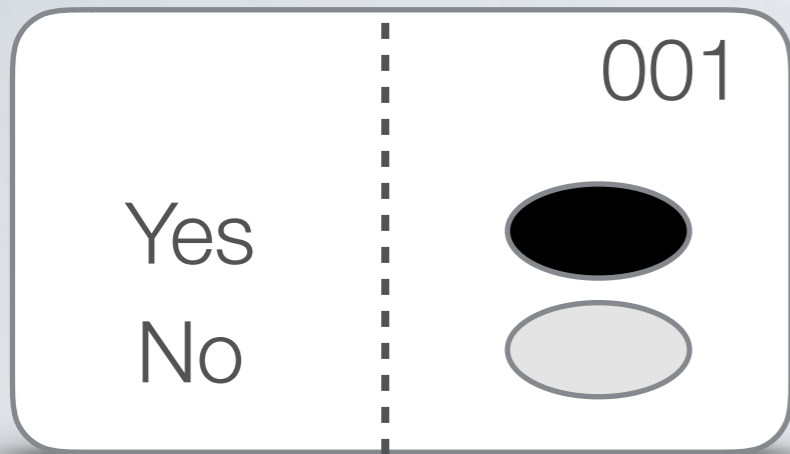
002.2		Yes
002.1		No
001.2		No
003.2		Yes
001.1	✓	Yes
003.1	✓	No



Honest
Quorum

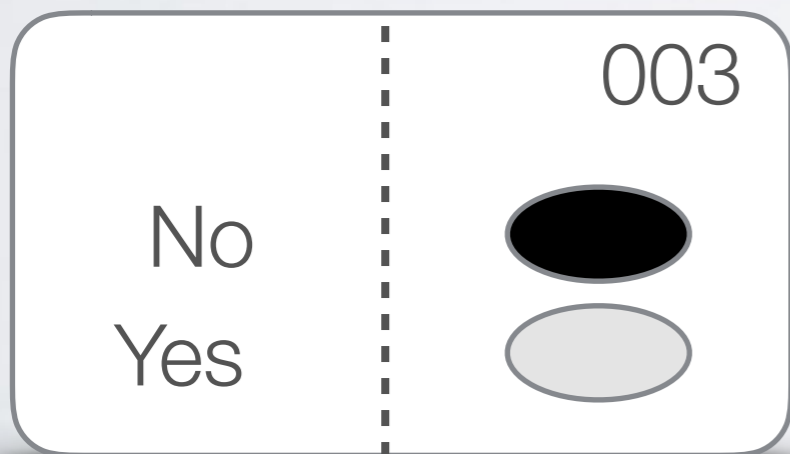
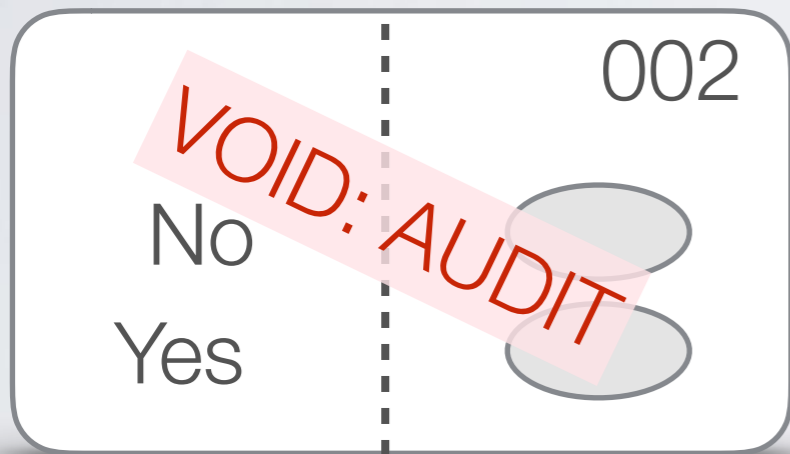
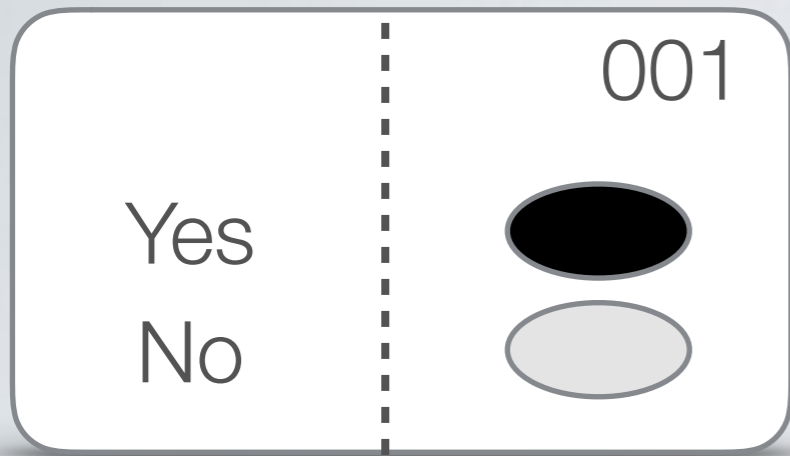
003.1	✓	No
001.2		No
002.2		Yes
003.2		Yes
001.1	✓	Yes
002.1		No

002.2		Yes
002.1		No
001.2		No
003.2		Yes
001.1	✓	Yes
003.1	✓	No



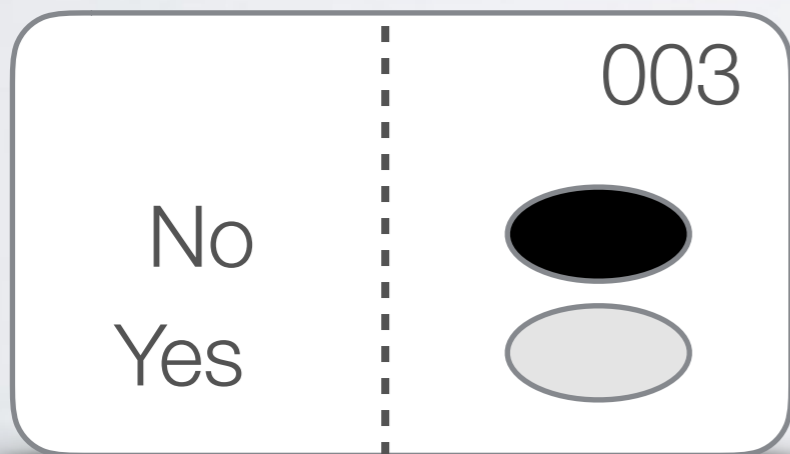
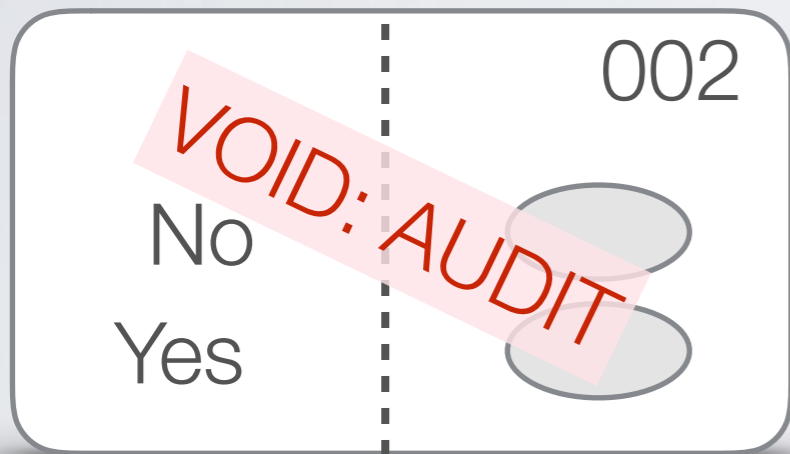
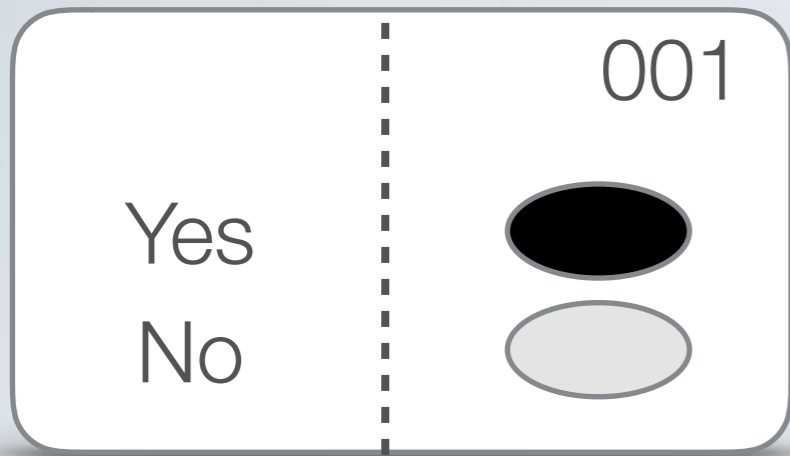
003.1	✓	No
001.2		No
002.2		Yes
003.2		Yes
001.1	✓	Yes
002.1		No

002.2		Yes
002.1		No
001.2		No
003.2		Yes
001.1	✓	Yes
003.1	✓	No



003.1	✓	No
001.2		No
002.2	↔	Yes
003.2		Yes
001.1	✓	Yes
002.1	↔	No

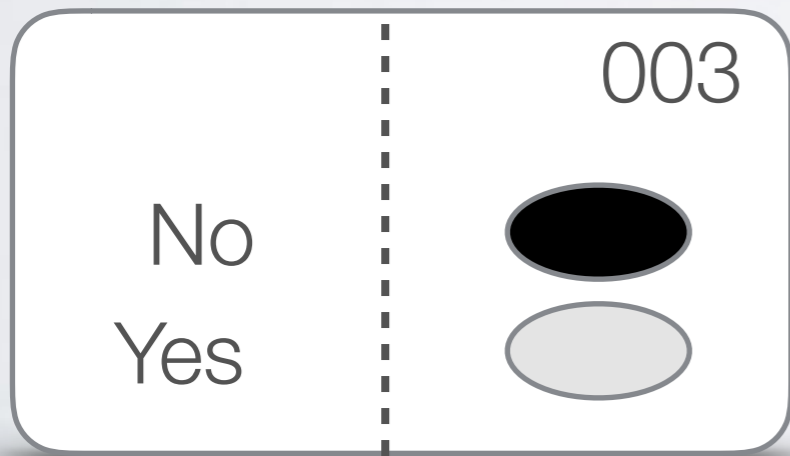
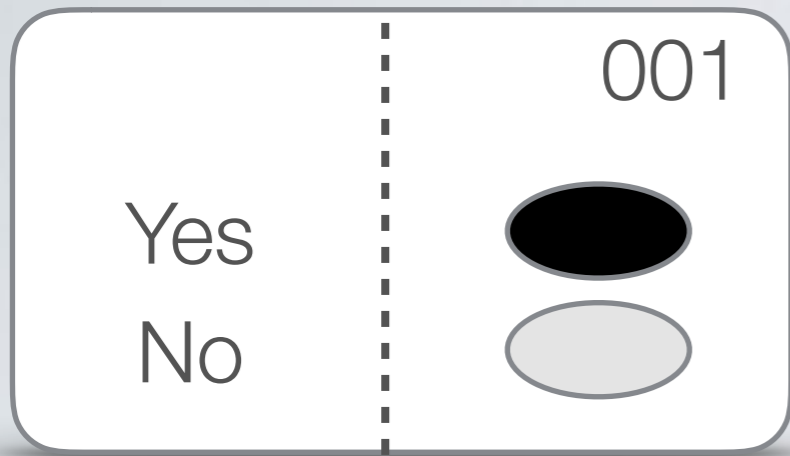
002.2	↔	Yes
002.1	↔	No
001.2		No
003.2		Yes
001.1	✓	Yes
003.1	✓	No



Corrupt

003.1	✓	No
001.2		No
002.2	↔	Yes
003.2		Yes
001.1	✓	Yes
002.1	↔	No

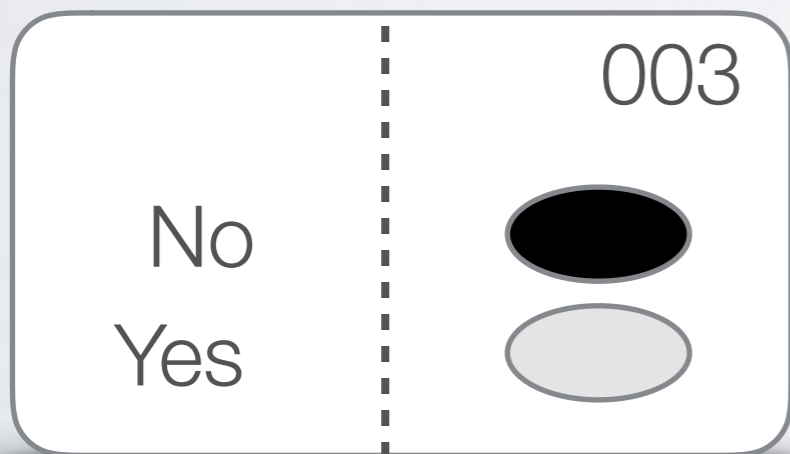
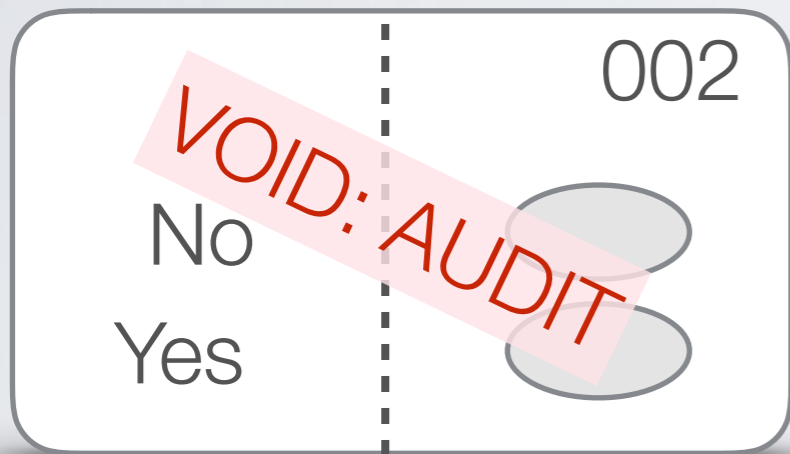
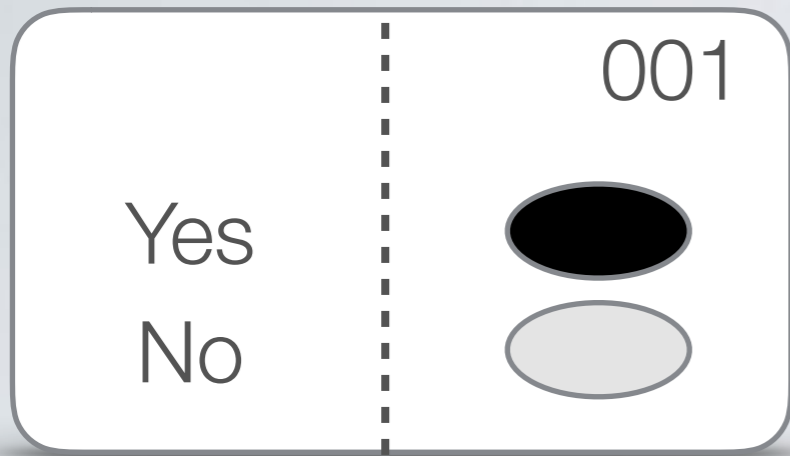
002.2	↔	Yes
002.1	↔	No
001.2		No
003.2		Yes
001.1	✓	Yes
003.1	✓	No



Corrupt

003.1	✓	No
001.2		No
002.2	↔	Yes
003.2		Yes
001.1	✓	Yes
002.1	↔	No

002.2	↔	Yes
002.1	↔	No
001.2		No
003.2		Yes
001.1	✓	Yes
003.1	✓	No



Corrupt

003.1	✓	No
001.2		No
002.2	↔	Yes
003.2		Yes
001.1	✓	Yes
002.1	↔	No

002.2	↔	Yes
002.1	↔	No
001.2		No
003.2	✓	Yes
001.1	✓	Yes
003.1		No

$$\begin{aligned}
 \Pr[\text{Detect}] &= 1 - 2^{-t} \\
 &= 99.9999\% \quad (t=20)
 \end{aligned}$$

003.1	✓	No
001.2		No
002.2	↔	Yes
003.2		Yes
001.1	✓	Yes
002.1	↔	No

002.2	↔	Yes
002.1	↔	No
001.2		No
003.2	✓	Yes
001.1	✓	Yes
003.1		No

Universal Verification

Should we care?

- * No: we already make collusion assumptions about election officials, so why not about verification?
- * No: breaking integrity is zero-sum for the parties, but breaking privacy might not be
- * Yes: auditing should be open to all, even non-voters
- * Yes: the trustworthiness of auditing should not rely on whether I trust a preselected set of entities or not



Questions?

@PulpSpy

<http://vaddr.space>